| + × +   | _   |   | × |   | ÷  |   | + |  |
|---|-----|---|---|---|----|---|---|--|
| $2(m+6) \qquad \qquad$   | +   | + |   | _ |    | × |   |  |
| -24 -24 -21.4 - |     |   | × |   | ÷  |   | + |  |
|   | +   | + |   | _ |    | × |   |  |
|   | -   |   | × |   | ÷. |   | + |  |
|   |     | + |   | _ |    | × |   |  |
| EVALACCIAAC   |     |   | × |   | ÷  |   | + |  |
|   |     |   |   | _ |    | × |   |  |
| 3(4x - 4)   |     |   | × |   | -  |   | + |  |
| $\delta n + 3 = 5$  |     |   |   | _ |    | × |   |  |
|   |     |   |   |   |    |   | + |  |
|   |     |   |   | - |    | × |   |  |
|   |     |   |   |   |    |   | + |  |
|   |     |   |   | - |    | × |   |  |
| 10 - 4x = 30  |     |   |   |   | ÷. |   | + |  |
|   |     |   |   | - |    | × |   |  |
|   | 11/ |   |   |   | ÷. |   | + |  |
| -7160 - 1   |     |   |   | - |    | × |   |  |
|   |     |   | , |   | +  |   | + |  |
| 10  |     |   |   | - |    | × |   |  |
|   |     |   |   |   |    |   |   |  |

# Student Booklet

+

 $\times$ 

 $\times$ 

+

\*

| Name    |
|---------|
| Teacher |
| Period  |

5(2h+4) = 40

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## Learning to Solve:

Use what you know about order of operations to simplify or evaluate.

| <b>1. A.</b> 2(6 – 4)    | <b>B.</b> 2(6) – 2(4)       |
|--------------------------|-----------------------------|
| <b>2. A.</b> 6(1 + 5)    | <b>B.</b> 6(1) + 6(5)       |
| <b>3. A.</b> (-3)(2 + 3) | <b>B.</b> (-3)(2) + (-3)(3) |
| <b>4. A.</b> 5(2 × 4)    | <b>B.</b> 5(2) × 5(4)       |
| <b>5. A.</b> 6(6 ÷ 2)    | <b>B.</b> 6(6) ÷ 6(2)       |



the distributive property without drawing a picture.

#### 3(x+5) = 3x + 15

## **Practicing Together:**

Simplify each algebraic expression.

**1.** 2(*m* + 6)

**2.** 3(4*g* + 7)

**3.** 8(*y* – 1)

**4.** (-5)(*d* + 3)

**5.** 9(2 + *k*)

**6.** –4(5*n* – 2)

#### **Trying It on Your Own**

**1.** Simplify (-2)(3*a* + 1)

**a.** –8*a* because you add 3*a* and 1 first in the parentheses before you multiply.

**b.** *a* – 1 because you add –2 to each of the terms in the parentheses to simplify.

**c.** -6a + 1 because you multiply -2 by 3a to simplify.

**d.** -6a + (-2) because you multiply -2 by each of the terms in the parentheses to simplify.

**2.** Simplify 9(*g* – 4)

**a.** 9*g* – 4 because you multiply 9 by the first term in the parentheses when they are close together.

**b.** 9g + 36 because you multiply 9 by both terms in the parentheses.

c. 9g – 36 because you multiply 9 by both terms in the parentheses.

**d.** *g* – 36 because you can multiply numbers together only when they are in parentheses.

#### **3.** Simplify 5(8 – *h*)

**a.** 40 – 5*h* because when you use the distributive property, you multiply 5 by both terms in the parentheses.

**b.** 40 – *h* because you multiply the 2 numbers that are next to each other with parentheses when you use the distributive property.

**c.** 8 – 5*h* because you multiply the variable by 5.

**d.** 13 + 5*h* because you add 5 to each of the numbers in the parentheses.

#### **4.** Simplify 6(*p* + 6)

**a.** 6p + 12 because you multiply 6 by the variable in the parentheses and add 6 to the number in the parentheses.

**b.** p + 12 because you can only add 6 to the number in the parentheses.

**c.** 6p + 36 because you multiply 6 by both terms in the parentheses.

**d.** p + 36 because you can only multiply 6 by the number in the parentheses.

# Wrapping It Up

Rewrite 47(35) + 47(15), using the distributive property of multiplication over addition.

## Warming Up:

Solve the problems.

**1.** Marci went to the ice cream store with 4 friends. All of them each ordered a sundae with 2 scoops of ice cream and various toppings. A sundae with 2 scoops of ice cream costs \$2.99, but the final cost of each sundae depended on the number of toppings added. The average cost, including sales tax, of the sundaes they ordered was \$3.73. What was the total cost for all 5 sundaes?

**2.** Sonia wants to make 10 bowls of peach punch and 15 bowls of pineapple punch. Each punch bowl holds 16 liters of punch. She needs 7 liters of soda to make each bowl of punch. How many liters of soda will Sonia need in all?

#### Learning to Solve:

Hot dogs cost \$1.25 and large soft drinks cost \$0.75 at the carnival. Jerome has to buy hot dogs and large drinks for 8 people. How much money does he need?

## **Practicing Together:**

Solve each problem.

**1.** Jacki took 3 of her friends to the movies. All 4 of them wanted a small bag of popcorn that cost \$2.75 each and a small drink that cost \$1.25 each. How much did they spend altogether on their drinks and popcorn?

**2.** Ken drew a picture of 2 rectangles. He wondered what the area of the combined rectangle would be. Find the areas. (Remember that the area of a rectangle is found by multiplying base times height.)



**3.** Bev said she could use the distributive property of multiplication over addition to help her multiply mixed numbers. Here is what she wrote:

$$3\frac{2}{3} \times 4\frac{1}{2} = (3 \times 4) + (\frac{2}{3} \times \frac{1}{2})$$
$$= 12 + \frac{1}{3}$$
$$= 12\frac{1}{3}$$

Is her method correct? Why or why not?

### **Trying It on Your Own**

Solve the problems on your own.

**1.** Kayla rewrote the expression (0.75)(45) + (0.75)(55) as 0.75(100). Do you agree with Kayla?

**a.** Yes, I agree with Kayla because she used 0.75 as a multiple.

**b.** Yes, I agree with Kayla because she can rewrite the original expression as 0.75(45 + 55).

c. No, I disagree because you have to do the operations in order in the expression.

**d.** No, I disagree because you get a different answer.

**2.** A school supply store sells pencils with matching erasers. Each pencil costs \$0.79 and the erasers are \$0.46 each. Tate bought 10 sets of pencils and erasers. Which expression shows the cost of the pencils and erasers that Tate bought?

**a.** 10 + 0.79 + 0.46 because you want to know the total cost, so you add the amounts.

**b.** 0.79(10 + 0.46) because each pencil costs \$0.79, so you need to multiply by 10.

c. 10(0.79 + 0.46) because you multiply the cost of each set by the number of sets.
d. (10)(0.79) + 0.46 because you multiply the cost of each set by the number of sets.

**3.** Carmen used the distributive property to multiply:

Do you agree with her work?

**a.** No, I do not agree because she used addition when she was supposed to multiply.

**b.** No, I do not agree because she should have written  $(30 + 150) \cdot (5 + 150)$ .

c. Yes, I agree because addition is the inverse of multiplication.

**d.** Yes, I agree because her method is equivalent to 150(30 + 5).

**4.** Sam wanted to find the combined area of 2 rectangular playgrounds that are connected to each other. What expression might Sam use to solve the problem?



**d.** 15(20) + 35

## Wrapping It Up

Solve the problem.

John simplified an algebraic expression by using the distributive property. His simplified expression was 12q + 24. What algebraic expression might he have simplified?

## Warming Up:

Evaluate each expression for u = 2.

**1.** 10 – 4*u* 

**2.** 4*u* – 10

**3.** 2*u* + 6 - 3 + 5*u* 

**4.** 9*u* – 3*u* – 3

**5.**7+6-7*u* 

#### Learning to Solve:

2 algebraic expressions are equivalent when the value of 1 expression equals the value of the other for all replacements of the variables.

| Value of the variable | 6 <i>n</i> | 4n + 2n |
|-----------------------|------------|---------|
| 2                     |            |         |
| -1                    |            |         |

The value of each of the following expressions is 4 when x = -2.

| 2 <i>x</i> + 8 | х+б | 2 – <i>x</i> | 2(x + 4) |
|----------------|-----|--------------|----------|
|                |     |              | · · ·    |

Evaluate these expressions for x = 2 and  $x = \frac{1}{2}$ .

|                  | Value of the variable |                   |  |
|------------------|-----------------------|-------------------|--|
| Expression       | x = 2                 | $x = \frac{1}{2}$ |  |
| 2 <i>x</i> + 8   |                       |                   |  |
| х + б            |                       |                   |  |
| 2 – <i>x</i>     |                       |                   |  |
| 2( <i>x</i> + 4) |                       |                   |  |

Which expressions have the same value when you substituted 2 and  $\frac{1}{2}$ ?

## **Practicing Together:**

Decide whether the expressions in the table are equivalent.

Write "Y" if the expressions are equivalent or "N" if the expressions are not equivalent.

| Expression 1            | <i>a</i> = 4 | Expression 2 | <i>a</i> = 4 | Equivalent |
|-------------------------|--------------|--------------|--------------|------------|
| 2 <i>a</i> + 3 <i>a</i> | a(2 + 3)     |              |              |            |
| 5a – 4a                 |              | 3a – 2a      |              |            |
| 5( <i>a</i> + 3)        | 8a           |              |              |            |
| 0.7 <i>a</i>            |              | a – 0.3a     |              |            |

#### **Trying It on Your Own**

**1.** Are 6(36 ÷ 2) and (6)36 ÷ (6)2 equivalent?

**a.** No, because the parentheses mean that you should divide each number by 6, not multiply.

**b.** No, because 6 is multiplied by the quotient, which results in a larger product than multiplying each term before dividing.

c. You cannot tell because you are supposed to do what is in the parentheses first.

**d.** This is impossible to do because you cannot combine multiplication and division.

**2.** Sammi found an expression equivalent to 36k - 48. Which expression might Sammi have found?

**a.** 3k - 4 because you can multiply both terms by 12 to get 36k - 48.

**b.** –12*k* because 36 – 48 = –12.

**c.** 12(3*k*) – 12(4) because 36*k* – 48 is the same as 12(3*k* – 4).

**d.** -4(9k + 12) because multiplying 12 by -4 will give a product of -48.

**3.** Jason said, "9t and 10t – 1 are equivalent." Megan disagreed. Who do you agree with? Why?

**a.** Jason because 10 – 1 = 9.

**b.** Jason because if t = 1, the 2 expressions have the same value.

**c.** Megan because the 2 expressions have the same value for only t = 1.

**d.** It is impossible to tell because you do not know the values for *t*.

**4.** Kim used -3 as the value for the variable in the expression 3 - 4x. Which of the following is the value she found?

**a.** 15 **b.** 9

**c.** –9

**d.** –15

# Wrapping It Up

Solve the problem.

Is 5b + 4b equivalent to 9b? Explain your answer.

## Warming Up:

Evaluate each expression by substituting 4 as the value for the variable.

**1.**5a

**2.** −*b* + 7

**3.**  $\frac{1}{2}x$ 

**4.**  $\frac{100}{m}$ 

**5.** –6.1*g* 

## Learning to Solve:

**1.** Simplify or evaluate the expression  $6 + 8 \div 2 \times 3 - 5$ .

In another class, 3 students solved the problem in a different way.

| A. One student solved it this way:            | $6+8\div 2\times 3-5$     |
|---|---------------------------|
|   | $14 \div 2 \times 3 - 5$  |
|   | 7 × 3 – 5                 |
|   | 21 – 5 = 16               |
| <b>B.</b> Another student solved it this way: | $6+8 \div 2 \times 3 - 5$ |
|   | 6 + 4 × 3 – 5             |
|   | 10 × 3 – 5                |
|   | 30 - 5 = 25               |
| <b>C.</b> A third student solved it this way: | $6+8 \div 2 \times 3 - 5$ |
|   | 6 + 8 ÷ 6 - 5             |
|   | 6 + 8 ÷ 1                 |
|   | 6 + 8 = 14                |

Write how you remember the order of operations.

2. What operations are in this expression?

$$\frac{-6y-3}{3}+2y$$

According to the order of operations, which operation could we perform first?

Evaluate the expression for the value of the variable.

$$\frac{-6y-3}{3}+2y$$

*y* = \_\_\_\_\_

# **Practicing Together:**

Work with your partner to complete the table by evaluating each expression for the indicated value.

|                  | Value of the variable |               |    |     |   |
|------------------|-----------------------|---------------|----|-----|---|
| Expression       | 2                     | <u>2</u><br>5 | -2 | 0.3 | 0 |
| 5x - 5 + 10x     |                       |               |    |     |   |
| h(10 + 25) – 10h |                       |               |    |     |   |

## **Trying It on Your Own**

Solve the problems on your own.

**1.** Evaluate the expression  $\frac{4b+8}{2} + 2b \times 5$  if b = 6.

**a.** 160 because you multiply 4 times 6 then divide by 2. After that, you do the computations from left to right.

**b.** 140 because you evaluate the numerator first, then divide. Next, add 12, and finally multiply by 5.

**c.** 88 because you do the multiplication in the numerator first, then divide 8 by 2. Next, you add 24 and 4, then add the product of 12 times 5.

**d.** 76 because you evaluate the numerator first, then divide. Next, multiply 12 times 5, and add the value from the division.

**2.** Which of the following values of the variable would give 34 for the expression 3x - 5x + 6(3 - x)?

- **a.** 3
- **b.** 1
- **c.** –2
- **d.** –5

**3.** Ted evaluated the expression 5x - 3(2x - 8) for x = 5. He got 19. Kennie said, "I disagree. I got 44." Who do you agree with?

**a.** I agree with Ted because he evaluated the expression in the parentheses, multiplied it by 3, and then subtracted that from 25.

**b.** I agree with Kennie because she evaluated 5*x* first, then subtracted 3. Her last step was to multiply by the value of the expression in the parentheses.

**c.** Neither answer is correct. The correct answer is 11 because you evaluate 5*x* first, then subtract the product of 3 and 2*x*. The last step is to subtract 8.

**d.** Both answers are possible because you can use the Order of Operations in different ways.

**4.** Which expression has the same value as the expression 7x + 3x - 2x - 7x, when x = 4?

**a.** 10x - 9 **b.** 2x - 4x + 3x **c.** 2x - 4(1 - 2x)**d.** 7x - 3x + 2x - 7x

# Wrapping It Up

Martha said that 3n + 8 has the same value as 6n + 2 for n = 2.

A. Is she correct?

B. Are the expressions equivalent?

## Warming Up:

Evaluate each expression for the given value.

**1.** 2*m* + 8 for *m* = 6

**2.** -3x + 4 for x = -5

**3.** 9*n* – 3 for  $n = \frac{1}{3}$ 

**4.** 2 + 5.5*g* for *g* = 2

#### Learning to Solve:

Each expression in the table is equal to 14. Find the value of the variable that will make this statement true.

| Value of the Expression is 14 |                   |  |  |
|-------------------------------|-------------------|--|--|
| Expression                    | Value of Variable |  |  |
| 7 <i>m</i> – 14               | <i>m</i> =        |  |  |
| 5 <i>y</i> + 4                | <i>y</i> =        |  |  |
| 6 + 8 <i>u</i>                | <i>u</i> =        |  |  |
| 4 <i>q</i> – 10               | <i>q</i> =        |  |  |

## **Practicing Together:**

Work with your partner to complete the table by finding the value of the variable that will make the expression equal to 10.

| Value of the Expression is 10 |                   |  |  |
|-------------------------------|-------------------|--|--|
| Expression                    | Value of Variable |  |  |
| 10 <i>a</i> + 5               | <i>a</i> =        |  |  |
| 2 <i>f</i> – 12               | f =               |  |  |
| 2( <i>g</i> + 2)              | <i>g</i> =        |  |  |
| 1 + 3e                        | e =               |  |  |
| 6x – 14                       | <i>x</i> =        |  |  |

## **Trying It on Your Own**

Solve the problems.

**1.** What value of the variable will make the expression 4r + 12 equal to 12?

- **a.** 0
- **b.** 3
- **c.** –4
- **d.** 4

**2.** What value of the variable will make the value of the expression 5h - 13 equal to 12?

- **a.** 1 because 1 minus 13 is 12.
- **b.** 5 because 25 13 is 12.
- **c.** 17 because 17 minus 5 is 12.
- **d.** 25 because 25 13 is 12.

**3.** Jon wants to find a value for the variable so that the expression 4(s + 4) equals 16. Which of the following describes a process he could use?

- **a.** Use the distributive property to get 4s + 4. 12 plus 4 is 16, so s must 12.
- **b.** Use the distributive property to get 4s + 16. 4 times 4 is 16, so s must be 4.
- **c.** Use inverse operations. 16 divided by 4 is 4, so *s* must be 4.
- **d.** Think about what number times 4 equals 16. *S* plus 4 must be 4, so *s* must be 0.

**4.** Corey wrote an expression that equaled 25 when the variable was 20. Which of the following expressions could Corey have written?

**a.** x + 2(30 - x) - 15 **b.** 10 - x + 2x **c.** 2x - 4(5x - 3x)**d.** 6x - 3(2x + 1)

# Wrapping It Up

Write an expression that equals 10 when the value of the variable is equal to 5.

## Warming Up:

Find the value of the variable that makes the expression equal to the value given.

**1.** c + 8; the expression equals 20. *c* = **2.** 10 - q; the expression equals -1. *g* = \_\_\_\_\_ **3.** -7(h); the expression equals 49. h =**4.**  $\frac{m}{6}$ ; the expression equals -8. *m* = \_\_\_\_\_ **5.**  $\frac{2}{9} + r$ ; the expression equals 1. *r* =

#### Learning to Solve:

The guess-and-test method.

Use this method to solve 5m - 3 = 22.

Let's try m = 4.

5(4) - 3 =

20 - 3 = 17

17 ≠ 22

Therefore, 4 is not a solution.

Because 17 is less than 22, let's substitute a larger value than 4 for the variable, m.

Let's try m = 5.

5(5) – 3 =

25 - 3 = 22

22 = 22

Use the guess-and-test method to find the missing number in the equations when given the value of the variable.

#### Problem 1:

3n - = 16 for n = 9

Substitute 9 for n in the term 3n.

3(9) – ? = 16

27 – ? = 16

Think about what number subtracted from 27 will equal 16. Be able to tell me how you got your answer.

27 – ? = 16 ? = \_\_\_\_

#### Problem 2:

17 = ? c + 8 for c = 1

Substitute 1 for c in the term <u>?</u>c.

? (1) + 8 = 17

Think about what number multiplied by 1 and then added to 8 will equal 17. Be able to explain how you found your answer.

? (1) + 8 = 17

? = \_\_\_\_\_
# **Practicing Together:**

Working with your partner, find a value for the variable or the missing value that will make the equation true in each problem.

**1.**8*m*−8 = 72

**2.** 
$$\frac{2x}{4} + 8 = 12$$

**3.** −8 = −10*g* + 12

**4.** 15 = 3d - 2 for d = 6

### Name: .

## **Trying It on Your Own**

```
1. Solve: 9r - 9 = 81

a. r = 10 because 90 - 9 = 81

b. r = 9 because 9 \cdot 9 = 81

c. r = 8 because 8 \cdot 9 = 72 and 72 + 9 = 81

d. r = 0 because 90 - 9 = 81
```

**2.** Denny solved the equation  $\frac{3x}{5} + 7 = 10$  by using guess-and-test. Which of the following could have been his process?

**a.** Think: What number added to 7 is 10? 3 + 7 = 10.  $\frac{3x}{5}$  must be 3, so x is 3.

**b.** Think: What number added to 7 is 10? 3 + 7 = 10.  $\frac{3x}{5}$  must be 3, so 3x is 15. 3 times 5 is 15, so x is 5.

**c.** Think: What number added to 7 is 10? 3 + 7 = 10.  $\frac{3x}{5}$  must be 3, so 3x is 3 and x is 1.

**d.** Think: What number added to 7 is 10? 3 + 7 = 10.  $\frac{3x}{5}$  must be 3, so 3x is 15. So x is 15.

- **3.** Find the missing value in the equation 4d ? = 16 for d = 6.
  - **a.** The missing value is 24 because 4d = 24 when d = 6.
  - **b.** The missing value is 40 because 16 + 24 = 40 when d = 6.
  - **c.** The missing value is 20 because 4 + 16 = 20 when d = 6.
  - **d.** The missing value is 8 because 24 8 = 16.

```
4. Solve the equation 30 = 10 − 4x.
a. x = −5 because 30 = 10 + 20.
```

- **a.** x = -5 because 50 = 10 + 20.
- **b.** *x* = 5 because 30 = 10 + 20.
- **c.** *x* = 10 because 30 = 10 40 .
- **d.** *x* = -10 because 30 = 40 10.

# Wrapping It Up

Orren said that the solution to 8n - 21 = -5 is n = 2.

Is he correct?

## Warming Up:

Use >, <, or = to make a true statement.

**1.** –254 \_\_\_\_\_ –256



**3.** (-12 • 6) • 2 \_\_\_\_\_ -12 • (6 • 2)

**4.** (−12 ÷ 6) ÷ 2 \_\_\_\_\_ −12 ÷ (6 ÷ 2)

# Learning to Solve:

Guess a reasonable value for *b*.

| Ь | 5 <i>b</i> + 11 | Does 5b + 11 = 1? |
|---|-----------------|-------------------|
|   |                 |                   |
|   |                 |                   |
|   |                 |                   |
|   |                 |                   |

*b* = \_\_\_\_\_

## **Practicing Together:**

1. Fill in the column headings.

**2.** Try different values to find the value of the variable that makes the equation true.

**Problem 1:** 2*h* – 9 = 13 *h* = \_\_\_\_\_



**Problem 2:** 7 + 3*u* = -20 *u* = \_\_\_\_\_

# **Trying It on Your Own**

**1.** Jeri used a table to solve the equation 9 = 3x + 2(6x - 3). She said the solution was x = 1. Do you agree with Jeri?

**a.** Yes, because when you use a table to solve the equation, the answer will be correct.

**b.** Yes, because when you substitute 1 for the variable, both sides of the equation equal 9.

c. No, because you cannot use a table to solve an equation with parentheses.

**d.** It is not possible to tell without seeing the table.

**2.** Derek started to make a table to solve the equation 5w + 2 + 7w = 50.

| Value of <i>w</i> | 5 <i>w</i> + 2 + 7 <i>w</i> | Does $5w + 2 + 7w = 50$ ? |
|-------------------|-----------------------------|---------------------------|
| 0                 | 2                           | No                        |

Which of the following describes how he might decide the next entry in his table?

**a.** He should pick a number between 0 and 10 because the value on the left side is too small.

**b.** He should pick a number between 0 and –10 because the value on the right side is too large.

**c.** He should pick a number between 10 and 50 because the value on the right side is 50.

**d.** He should pick a number larger than 50 because the value on the left side was too small.

Use this table to answer problems 3 and 4.

### Solve the equation 3(4x - 2) - 8 = 10.

| Value of <i>x</i> | 3(4x-2)-8 |  |
|-------------------|-----------|--|
| -1                | -26       |  |
| 0                 | -2        |  |
| 1                 | -2        |  |
| 2                 | 10        |  |
| 3                 | 22        |  |

3. Which row in the table has a computation error?

**a.** When x = -1, the value of 3(4x - 2) - 8 should be -2.

**b.** When x = 0, the value of 3(4x - 2) - 8 should be -14.

**c.** When x = 1, the value of 3(4x - 2) - 8 should be -14.

**d.** When x = 3, the value of 3(4x - 2) - 8 should be -22.

**4.** What is the solution to the equation 10 = 3(4x - 2) - 8?

- **a.** The solution to the equation is not given in the table.
- **b.** x = 10 because that is the value on the left side of the equation.
- **c.** x = 1 because then 3(4x 2) 8 equals 10.
- **d.** x = 2 because the value of 3(4x 2) 8 is 10.

# Wrapping It Up

So far, you have learned 2 methods for solving equations—the guess-and-test method and the table method. Compare these methods. Write 1 thing that is similar about these methods and 1 thing that is different.

Similar:

Different:

# Warming Up:

Graph and label the coordinate points.

| A (7, 4) | B (3, 5) | C (4, -4) |
|----------|----------|-----------|
|          |          |           |

- D (-6, 1) E (-2, -2) F (0, 9)
- G (-5, 8) H (-1, 0)



# Learning to Solve:

**Problem 1:** 2x - 3 = 5

| X | 2 <i>x</i> – 3 |
|---|----------------|
| 0 |                |
| 1 |                |
| 2 |                |

Graph the points on the coordinate grid. Connect them by drawing a line through the points.



How can we use this line, the graph of the expression 2x - 3, to determine the value of x that will make the equation 2x - 3 = 5 true?

*x* =

## **Practicing Together:**

### *If using a graphing calculator:*

Working with your partner, solve the problems, using your graphing calculators.

Find the value of x that makes the equation 4x + 1 = -7 true.

1. What equations will you graph?

Y = \_\_\_\_\_

Y = \_\_\_\_\_

2. Graph the equation on your graphing calculator and then sketch it below.



**3.** Write the solution to the equation.

Find the solution to the equation 5 = 5(x + 3).

4. What equations will you graph?

Y = \_\_\_\_\_

Υ = \_\_\_\_\_

5. Graph the equation on your graphing calculator and then sketch it below.



**6.** Write the solution to the equation.

### *If not using a graphing calculator:*

Working with your partner, solve the problems, using the graphing method.

Find the value of *d* that makes the equation 4d + 1 = -7 true.

**1.** Select values for *d* and fill in the table with those values.

**2.** Write the coordinate points in the table.

| Variable | Expression | Ordered Pair |
|----------|------------|--------------|
|          |            |              |
|          |            |              |
|          |            |              |
|          |            |              |

### **3.** Graph the points on the coordinate grid.



**4.** Draw a line connecting the points.

**5.** For 4*d* + 1 to equal –7, *d* =

## **Trying It on Your Own**

### *If using a graphing calculator:*

Find the solution to the equation 3x - 4 = -7, using your graphing calculators.

1. What equations would Shannon graph to solve the equation?

**a.** Y = 3x + 4 and Y = 7 **b.** Y = -3x + 4 and Y = -7 **c.** Y = 3x - 4 and Y = -7**d.** Y = 3x - 4 and Y = 7

# 2. Which of the following 4 graphs would Shannon use to solve the equation?









3x - 4 = -7

**3.** What is the coordinate of the point where the lines intersect that will make the equation true?

**a.** (-1, 7) **b.** (7, -1) **c.** (1, -7) **d.** (-1, -7)

4. What is the solution to the equation?

**a.** The solution to the equation is x = -1.

**b.** The solution to the equation is x = 1.

**c.** The solution to the equation is x = -7.

**d.** The solution to the equation is x = 7.

### *If not using a graphing calculator:*

Find the solution to the equation 3g - 4 = -7, using the graph method.

**1.** Shannon completed her table to find values for g and the expression 3g - 4. Which of the following is a table Shannon could have made?

| a. | Value of g | Value of 3 <i>g</i> – 4 | b. | Value of g | Value of 3 <i>g</i> – 4 |
|----|------------|-------------------------|----|------------|-------------------------|
|    | 0          | -4                      |    | 0          | 4                       |
|    | -1         | 1                       |    | 1          | 1                       |
|    | -2         | 2                       |    | 2          | 2                       |

| c. | Value of <i>g</i> | Value of 3 <i>g</i> – 4 | d. | Value of g | Value of 3 <i>g</i> – 4 |
|----|-------------------|-------------------------|----|------------|-------------------------|
|    | 0                 | -4                      |    | 0          | 4                       |
|    | -1                | -7                      |    | 1          | -1                      |
|    | -2                | -10                     |    | 2          | 2                       |

2. What are the coordinate points for her graph?

**a.** (0, -4); (-1, 1); (-2, 2) **b.** (0, 4); (1, 1); (2, 2) **c.** (0, -4); (-1, -7); (-2, -10) **d.** (0, 4); (1, -1); (2, 2)

### 3. Which of the following 4 graphs would she use?









- 4. What is the solution to the equation?
  - **a.** The solution is g = 3.
  - **b.** The solution is g = -3.
  - **c.** The solution is g = 1.
  - **d.** The solution is g = -1.

# Wrapping It Up

By graphing a line for an equation, Sterling found the solution of an equation was 3. What might the equation be?

# Warming Up:

**1.** Using the diagram of a scale below, determine how many circles are equal to a box. Remove boxes and circles until you have only 1 box on 1 side of the scale.

**2.** As you solve this problem, write the steps that you took. For example, for step 1, you could write, "I removed 3 circles from each side of the scale."





| Symbol                    | Meaning   |  |
|---------------------------|---|--|
| A <sub>3</sub>            | Add 3   |  |
| S <sub>3</sub> Subtract 3 |   |  |
| M <sub>3</sub>            | Multiply by 3   |  |
| D <sub>3</sub>            | Divide by 3   |  |
| DPMA                      | Distributive property of multiplication over addition |  |

# **Practicing Together:**

**1.** Draw squares to represent the variable and circles to represent the constant number in each expression of the equation.

- 2. Show each of your steps on the scale.
- **3.** Write the symbolic representation of each step below the scales.
- **4.** Solve for the variable.

$$7 + 2x = 19$$


## **Trying It on Your Own**

**1.** Which diagram could be used to solve the equation 3k + 10 = 16?



Use the diagram selected for problem 1 to solve problems 2 through 4.

**2.** For the first step, Penny removed the constant from both sides of the diagram. Which of the following would show that step?

**a.** A<sub>10</sub> **b.** S<sub>10</sub> **c.** D<sub>10</sub> **d.** M<sub>10</sub>

**3.** For the second step, Penny regrouped the symbols on the right side of the diagram. Which of the following would show that step?



- **b.** S<sub>3</sub>
- **c.** M<sub>3</sub>
- **d.** D<sub>3</sub>

- 4. What is the solution to the equation?
  - **a.** The solution to the equation is k = 16.
  - **b.** The solution to the equation is k = 10.
  - **c.** The solution to the equation is k = 3.
  - **d.** The solution to the equation is k = 2.

# Wrapping It Up

Perform the operation indicated. Express your answer in simplified form.

**1.** Subtract 5 from 3*n* + 5.

**2.** Add 7 to 2*m*.

**3.** Subtract *d* from 4*d* – 9.

### Warming Up:

In the pyramid below, the number in a box is the sum of the two numbers in white boxes above it. For example, 18 = 6 + 12. Fill in the blank in this pyramid.

| x |    | 6  |    | 12 |
|---|----|----|----|----|
|   | 11 |    | 18 |    |
|   |    | 29 |    |    |

### Learning to Solve:

2 less than the product of 9 times a number is equal to 16. What is the number?

**1.** Write an equation to help solve the problem.

**2.** Solve the equation by working backward.

To solve this equation, I will start with 16 and undo the operations.



### **Practicing Together:**

For each problem, complete the following 3 steps:

- **A.** Write an equation to help solve the problem (if needed).
- **B.** In the boxes, write the working backward steps you used to solve the problem.
- **C.** Write the solution to the equation.
- **1.** 3 added to 7 times a number is equal to 17.

Α.





С.



С.



С.

### **Trying It on Your Own**

Solve the problems on your own.

**1.** The difference of 5 times a number and 6 is equal to 19. Which equation could be used to solve this problem?

**a.** 5m ÷ 6 = 19 **b.** 5m − 6 = 19 **c.** 5m + 6 = 19 **d.** 5m • 6 = 19

**2.** Sam worked backward to solve the equation 45 = 4d + 9. Which of the following could describe his thinking?

**a.** First, because 9 is added to 4*d*, add 9 to 45. Then, divide the sum by 4 because 4*d* means multiplication.

**b.** First, because 9 is added to 4*d*, subtract it from 45. Then, divide the difference by 4 because 4*d* means multiplication.

**c.** First, because 4 is multiplied by *d*, divide by 4. Then, because 9 is being added, subtract it from 45.

**d.** First, because 4 is multiplied by *d*, multiply 45 by 4. Then, because 9 is being added, add 9 to the product.

**3.** Solve by working backward: 8h + 3 = 27.

**a.** First, add 3 to 27. Then, subtract 8 from 30. The solution is h = 22.

**b.** First, think that if 3 is added to 8h, then subtract it from 27. Then, because 8 is multiplied by h, multiply it by 24. The solution is h = 192.

**c.** First, think that if 3 is added to 8*h*, then subtract it from 27. Then, because 8 is multiplied by *h*, divide it into 24. The solution is h = 3.

**d.** First, think that if 8 is multiplied by h, divide 8h by 8. Then, subtract 3 from 27. The solution is h = 24.

**4.** Karen solved 6 = 3h - 15. Which of the following might be the first step she used when working backward?

- **a.** Think, if *h* is multiplied by 3, divide by 3.
- **b.** Think, if *h* is multiplied by 3, multiply 6 by 3.
- c. Think, if 15 is being subtracted, subtract it from 6.
- **d.** Think, if 15 is being subtracted, add it to 6.

# Wrapping It Up

I am thinking of a number. If I multiply the sum of my number and 6 by 3 and then add 9, the result is 33. What is my number?

## Warming Up:

Solve each equation using any method you prefer.

**1.** 3*m* + 1 = 4

**2.** 2 + 7*x* = 16

**3.** 10 = 4*r* − 2

**4.** 5*g* − 4 = 6

**5.** 3 = 2h - 1

### Learning to Solve:

We learned 5 different methods to solve equations:

- 1. Guess-and-test
- 2. Create a table
- 3. Draw a graph
- 4. Draw a diagram
- 5. Work backward

Use the method given to find the value of the variable that makes the equation true.

### 1. *Method:* Guess and test

13 = 4p - 3

### 2. Method: Create a table

### 5 + 2j = -1

| j | 5 + 2 <i>j</i> |
|---|----------------|
|   |                |
|   |                |
|   |                |
|   |                |

### 3. Method: Draw a graph

### 5d + 3 = -7





### **Trying It on Your Own**

Work on your own to solve the problems.

**1.** Kim solved the equation 3n - 9 = -3 by using a graph. What is the ordered pair that gives the solution to the equation?

**a.** (-3, 2) **b.** (2, -3) **c.** (3, -2) **d.** (-2, -3)

**2.** Stephen solved the equation -1 = 5u + 4 by working backward. Which of the following could be Stephen's first step?

**a.** Because 4 is added on the right side, add 4 on the right side to undo the addition.

**b.** Because *u* is being multiplied by 5, divide it by 5 to undo the multiplication.

**c.** Because *u* is being multiplied by 5, divide –1 by 5 to undo undo the multiplication.

**d.** Because 4 is added on the right side, subtract 4 from –1 to undo the addition.

**3.** Carmen solved the equation 6 = 6y - 24 by guess-and-test. Which of the following is the solution to the equation?

**a.** The solution is y = 24.

**b.** The solution is y = 6.

**c.** The solution is y = 5.

**d.** The solution is y = 4.

**4.** Ken solved the equation 12f - 6 = 0 by using a table. What value of the variable would make the equation true?



**b.** 0.5

**c.**  $1\frac{1}{2}$ 

**d.** 2

## Wrapping It Up

Write an equation whose solution is 3.

## Warming Up:

Write an algebraic expression that can be simplified to 48 - 8x.

### Learning to Solve:

The cost of a piece of nautical rope at Sam's Fish Shop is \$5 for the first foot and then \$2 per each foot after that. Sam will make a profit only if the total cost is greater than \$17. How much rope will Sam need to sell to make a profit?

1. What is the problem asking us to find?

2. What expression would we write to represent the cost of rope at Sam's Fish Shop?

**3.** How would we write the relationship to show the number of feet that needs to be sold to make a profit?

**4.** Working with your partner, find values for *n* that make the inequality 2n + 5 > 17 a true statement.

| Values for <i>n</i>           |  |  |  |  |
|-------------------------------|--|--|--|--|
| that make 2 <i>n</i> + 5 > 17 |  |  |  |  |
| a true statement              |  |  |  |  |
|                               |  |  |  |  |
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|                               |  |  |  |  |

**5.** Write the solution to the inequality.



### **Practicing Together:**

Working with your partner, solve each problem by using any method you prefer.

*Solve:* 4 + 5*g* ≤ 9

**1.** Solve for the variable. Write the solution.

2. Represent the solution on a number line.



**3.** Select a value from your graph that makes the inequality true. Substitute it into the inequality to show that it makes the inequality true.

**4.** Select a value from your graph that makes the inequality false. Substitute it into the inequality to show that it makes the inequality false.

*Solve:* 7*h* – 6 > 15

5. Solve for the variable. Write the solution.

6. Represent the solution on a number line.



**7.** Select a value from your graph that makes the inequality true. Substitute it into the inequality to show that it makes the inequality true.

**8.** Select a value from your graph that makes the inequality false. Substitute it into the inequality to show that it makes the inequality false.

#### Name: .

### **Trying It on Your Own**

**1.** Jessica solved the inequality  $2k + 15 \ge 25$ . Which of the following describes the solution to her inequality?

- **a.** All values of *k* that are greater than or equal to 25 will make the inequality true.
- **b.** All values of *k* that are greater than 10 will make the inequality true.
- **c.** All values of *k* that are greater than or equal to 5 will make the inequality true.
- **d.** All the values of *k* that are greater than 5 will make the inequality true.





**3.** Terry solved the inequality 4t - 3 < 13. Which of the following describes the solution to her inequality?

**a.** All values of *t* that are greater than 4.

**b.** All values of *t* that are less than 4.

**c.** All values of *t* that are less than 13.

**d.** All values of *t* that are greater than –13.





# Wrapping It Up

Oscar is thinking about selling custom-made T-shirts for \$8 plus \$3 for each word printed on the shirt. He wants to sell each T-shirt for \$20 or more. He wants to know how many words have to be printed on the shirt to sell them for \$20 or more.

He found an inequality to model the problem. He let x = the number of words. He wrote:  $3x + 8 \ge 20$ . He said that if  $x \ge 4$ , the inequity would be true. What does that mean?

## Warming Up:

Simplify each expression.

**1.** 3(*x* + 5)

**2.** 4(*m* − 2)

**3.** –2(6*p* + 1)

### Learning to Solve:

3(d+2) = 12

We will represent d + 2 as

Draw a representation of 3(d + 2) = 12 on the scale. Write "3(d + 2)," "=," and "12" below the appropriate section of the scale.



Use your diagram to find the value of *d* that makes the equation 3d + 6 = 12 a true statement.



8 = 8(h - 4)

Step 1: What is the first step?

What is the equation now?

Step 2: What is the next step?

Show this step:

What is the equation now?

Step 3: What is the next step?

What is the value of *h*?

### **Practicing Together:**

Working with your partner, solve each problem by using any method you prefer.

**1.** 4(*m* + 7) = 48

**2.** 20 – 2(*r* – 6)

**3.** 40 = 5(2*h* + 4)

**4.** −3(*n* − 1) = 9

Name: .

### **Trying It on Your Own**

**1.** Damon solved the equation 3(2k + 1) = 21. Which of the following describes accurate thinking about the solution process?

**a.** Because 21 is the product of 3 and some quantity, the quantity 2k + 1 must be

7. Because some quantity plus 1 is 7, 2k must be 6. 2 times a number is 6, so k must be 3.

**b.** First, you have to multiply 3 by 2*k*. Then, multiply 3 by 1. Next, you add 3 to 21 to get 24. 6*k* is 24, so *k* must be 4.

**c.** Because 21 is the product of 3 and some quantity, the quantity has to be 7. So *k* must be 7.

**d.** First, you multiply 3 by 1 by the distributive property. Then, you subtract 3 from 21 to get 18. 2*k* must be 18, so *k* is 9.

**2.** Keith solved the equation -4(p - 9) = 40. Which of the following describes accurate thinking about the solution process?

**a.** Keith used the distributive property to multiply –4 by *p* and 9. He got 4p - 36 = 40. Then, he used the inverse of subtraction to add 36. 4p = 76. Then, he used the inverse of multiplication to divide, so p = 19.

**b.** Keith used the distributive property to multiply 4 by *p* and 9. He got 4p + 36 = 40. He used the inverse to add 36. He got 4p = 76. He knows that *p* must be 19.

**c.** Keith rewrote the expression as -4(p + (-9)). Then, he used the distributive property to get -4p + 36 = 40. He used the inverse of addition to get -4p = 4. He used the inverse of multiplication to get p = -1.

**d.** Keith rewrote the expression as 4(p + 9). Then, he used the distributive property to get 4p + 36 = 40. He used the inverse of addition to get 4p = 4. Then, he knew that p must be 1.

**3.** Amy solved an equation and got a solution of n = 3. Which of the following equations could she have solved?

**a.** 3 = 3(n - 1) **b.** 3 = 3(3n + 3) **c.** 8 = 2(n + 1)**d.** 8 = -4(n - 1)

**4.** Mari solved an equation and got a solution of h = -2. Which of the following equations could she have solved?

**a.** 2(h - 2) = -2 **b.** 3(h - 3) = -15 **c.** 5(h + 2) = -8**d.** -2(h - 1) = -2

## Wrapping It Up

After applying the distributive property, an expression is 8x + 36. What might the expression have been before applying the distributive property?
# Warming Up:

**1.** The price to rent a roller-skating rink is a flat fee of \$150, plus \$4 per person invited. Shannon's parents are renting the rink to celebrate her 13th birthday. Write an expression for the total rental fee when *r* is the number of people invited.

# Learning to Solve:

Shannon wants to invite 10 people to her skating party. What will be the fee for the party?

The formula:  $4r + 150 = \cos t$  of party

1. What does *r* represent?

2. What does r equal in this problem?

3. How you will solve this problem and calculate the rental fee?

|   | Expressions and Equations 2: Les       |
|---|--|
| Name:   |  |
| Find the number of people invited to a roller-ska | ting party if the total cost is \$222. |
| <i>The formula:</i> cost of party = $4r + 150$    |  |
| What is the problem asking us to find?            |  |
|   |  |
|   |  |
| How is this represented in the formula?           |  |
|   |  |
|   |  |
| What is the new equation?                         |  |
|   |  |
|   |  |
| Solution steps:                                   |  |
| 5014101131203.                                    |  |
|   |  |
|   |  |
| What does this value of <i>r</i> indicate?        |  |
|   |  |
|   |  |

Name: .

# **Practicing Together:**

Working with your partner, solve each problem.

The formula for the area of a trapezoid is  $A = \frac{h(b_1 + b_2)}{2}$  where *h* refers to the height of the trapezoid,  $b_1$  refers to the length of 1 base, and  $b_2$  refers to the length of the second base.

Use the formula to find the missing values.

**1.** Find the area of the trapezoid.



2. The area of this trapezoid is 8.505 square inches. Find the height.



**3.** The area of this trapezoid is 30.8 square feet. Find the length of the base  $b_1$ .



**4.** Write a problem that someone could use this formula to solve: distance = (rate)(time).

#### **Trying It on Your Own**

The formula for the volume of a rectangular prism is V = lwh where *l* is the length, *w* is the width, and *h* is the height.

Volume is expressed in cubic units.

A cereal manufacturer wants to put a volume of 252 cubic inches of a new cereal in a box. The length of the box is 7 inches and the width is 3 inches. How tall must the box be?

1. Which of the following describes how you might solve the problem?

**a.** The formula says to multiply the length and the width. I would multiply 7 by 3 to find the height.

**b.** The formula says that the volume is the product of length, width, and height. I would multiply 7 by 3 by 252.

**c.** The formula says that the volume is the product of length, width, and height. I would multiply 7 by 3 and then divide 252 by that product to find the height.

**d.** The formula says to multiply the length and the width. I would multiply 7 by 3 to find the height and then use the inverse operation.

2. Which of the following gives the equation that could be used to solve the problem?

**a.** Let k = the height of the box in inches. 252 = 73k.

**b.** Let k = the height of the box in inches.  $252 = (7 \cdot 3)k$ .

**c.** Let k = the height of the box in inches. 252 • 7 • 3 = k.

**d.** Let k = the height of the box in inches. 7 • 3 = 252k.

- 3. Which of the following gives the property you used to solve the equation you created?
  - a. Division property of equality
  - **b.** Commutative property of multiplication
  - c. Distributive property of multiplication over addition
  - d. Associative property of multiplication

4. Which of the following gives the solution to the problem?

**a.** k = 3.45 inches **b.** k = 5,292 inches **c.** k = 0.08333 inches **d.** k = 12 inches

# Wrapping It Up



All edges of a cube are the same length. The formula for the volume of a cube is V = lwh, where V stands for volume, l stands for length, w stands for width, and h stands for height.

V = lwh

Solve this problem:

The edge of a cube measures 8 centimeters. What is the volume of the cube?

#### Warming Up:

Marcia is building a rectangular sandbox for her children. She wants the dimensions of the sandbox to be 8 feet by 6 feet. The height of the sandbox from the grass is 0.5 feet.

**1.** How many feet of lumber will she need to build the edges of the sandbox?

2. How much area of the yard will be covered by the sandbox?

**3.** How much sand will she need to buy to fill in the sandbox?

You may want to use the following formulas to help you solve these 3 problems:

**Area of a rectangle** = (length)(width)

**Perimeter of a rectangle** = 2(length) + 2(width)

**Volume of a rectangle** = (length)(width)(height)





5. Find the total surface area of this square pyramid.

#### **Practicing Together:**

Solve each problem. Round your answer to the hundredths place.

#### Formulas:

 $\pi = 3.14$ 

Area of a circle =  $\pi r^2$  (r indicates the value of the radius of the circle)



Area of an ellipse =  $\pi r_1 r_2$  ( $r_1$  indicates the value of 1 radius and  $r_2$  indicates the other radius)



**1.** Albert is installing a circular hot tub on his back deck. The hot tub will have a radius of 3.25 feet. What area of the deck will be covered by the hot tub?



**2.** Now Albert is thinking about installing an elliptical hot tub instead of a circular hot tub. Does the elliptical or circular hot tub have the larger area? By how much is the area larger?



#### Name:

# **Trying It on Your Own**

The formula for the volume of a triangular prism is  $V = \frac{1}{2}bhl$  where b is the length of the triangle base, h is the height of the triangle base, and l is the length of the prism.

The volume of a triangular prism is 60 cubic centimeters. The length of the triangle base is 4 centimeters and the height is 3 centimeters. How long is the prism?



1. Which of the following describes how you might solve the problem?

**a.** The formula says to multiply the base and the height and the length by  $\frac{1}{2}$ . I would multiply 4 by 3 by 60 by  $\frac{1}{2}$  to find the length.

**b.** The formula says that the volume is the product of base, height, and length.I would multiply 4 by 3 by 60.

**c.** The formula says that the volume is the product of  $\frac{1}{2}$ , base, height, and length. I would multiply  $\frac{1}{2}$  by 4 by 3 to find the length.

**d.** The formula says to multiply  $\frac{1}{2}$  by the base by the height by the length. I would multiply  $\frac{1}{2}$  by 4 by 3 and then divide 60 by the product to find the length.

#### Name: .

2. Which of the following gives the equation that could be used to solve the problem?

**a.** Let p = the length of the prism in centimeters.  $60 = \frac{1}{2} \cdot 43 \cdot p$ .

**b.** Let p = the length of the prism in centimeters.  $\frac{1}{2} \cdot 4 \cdot 3 \cdot p = 60$ .

**c.** Let p = the length of the prism in centimeters.  $4 \cdot 3 \cdot 60 \cdot \frac{1}{2} = p$ .

**d.** Let p = the length of the prism in centimeters.  $\frac{1}{2} \cdot 4 \cdot 3 = p$ .

3. Which of the following gives the solution to the problem?

a. p = 10 centimeters
 b. p = 6 centimeters
 c. p = 360 centimeters

**d.** *p* = 2.8 centimeters

**4.** π = 3.14

Area of a circle =  $\pi r^2$  (r indicates the value of the radius of the circle)



Jane was planning to make a circular garden. Her garden would have a radius of 4 ft. What would be the area of her garden?

**a.** 50.24 ft<sup>2</sup> **b.** 6.28 ft<sup>2</sup> **c.** 25.12 ft<sup>2</sup> **d.** 12.56 ft<sup>2</sup>

# Appendices

# EXPRESSIONS





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#### Warming Up:

Solve the problems.

**1.** Use order of operations to simplify 3(2 - 1) + 5.

**2.** Use order of operations to simplify 5 - 2(3 + 4).

**3.** Evaluate the expression 5p - 4 for p = 2.

**4.** Evaluate the expression -3 - 4x for x = -1.

**5.** Plot these points on the number line: 3, -4, 5.5, and 8.



# Learning to Solve:

| 7 + 2e            |                         |  |
|-------------------|-------------------------|--|
| Value of <i>e</i> | Value of 7 + 2 <i>e</i> |  |
| 6                 |                         |  |
| 7                 |                         |  |
| 8                 |                         |  |
| 9                 |                         |  |

Fill in the table by evaluating the expression 7 + 2e using the numbers 5, 10, 15, and 20.

| 7 + 2e            |                         |  |
|-------------------|-------------------------|--|
| Value of <i>e</i> | Value of 7 + 2 <i>e</i> |  |
| 5                 |                         |  |
| 10                |                         |  |
| 15                |                         |  |
| 20                |                         |  |

# **Practicing Together:**

Working with your group, evaluate the expression in each table, using 1 of the sets of variable values provided, and describe the pattern.

Set A variable values: -2, 1, 4, and 7

- OR -

Set B variable values: -2, 0, 2, and 4

| 5 <i>n</i> + 9    |                         |  |
|-------------------|-------------------------|--|
| Value of <i>n</i> | Value of 5 <i>n</i> + 9 |  |
|                   |                         |  |
|                   |                         |  |
|                   |                         |  |
|                   |                         |  |

# Set A variable values: -3, 0, 3, and 6

- OR -

# Set B variable values: -3, -2, -1, and 0

| 4 – 3 <i>a</i>    |                         |  |
|-------------------|-------------------------|--|
| Value of <i>a</i> | Value of 4 – 3 <i>a</i> |  |
|                   |                         |  |
|                   |                         |  |
|                   |                         |  |
|                   |                         |  |

# **Trying It on Your Own**

**1.** Using the values 1, 3, 5, and 7 for the values of the variable *f*, find the value of the expression 3f - 10.

**a.** 7, 1, -5, and -11 **b.** 13, 19, 25, and 31 **c.** -7, -1, 5, and 11 **d.** 3, 9, 15, and 21

2. By what value do the numbers 2, 7, 12, and 17 increase?

- **a.** 2
- **b.** 5
- **c.** 10
- **d.** –5

**3.** Using the values 2, 4, 6, and 8, the values of the expression 4h + 4 are 12, 20, 28, and 36. What is the pattern?

**a.** As the value of the variable increases by 2, the value of the expression increases by 8.

**b.** If the value of the variable is even, the value of the expression increases by 8.

**c.** As the value of the variable increases by 2, the value of the expression increases by 4.

**d.** As the value of the variable is multiplied by 2, the value of the expression increases by 8.

**4.** Using the values 1, 2, 3, and 4 for the variable *y*, what is the pattern of the expression 5y + 2?

- **a.** As the value of the variable increases by 1, the expression increases by 2.
- **b.** As the value of the variable increases by 1, the expression increases by 5.
- c. As the value of the variable increases by 1, the expression increases by 7.
- **d.** As the value of the variable increases by 1, the expression increases by 8.

# Wrapping It Up

Find an expression whose value is 7 if the value of the variable x is 1.

| ?                 |                     |  |
|-------------------|---------------------|--|
| Value of <i>k</i> | Value of expression |  |
| 1                 | 7                   |  |

# Warming Up:

Translate the phrases into algebraic expressions.

**1.** The quotient of 22 and *p*.

**2.** 8 less than the product of *z* and 10.

**3.** The sum of 12 and *a*.

**4.** 5 more than twice *d*.

**5.** *y* decreased by 6.

# Learning to Solve:

**1.** Write the algebraic equation for each sentence in the table.

| Sentence  | Algebraic Equation |  |  |
|---|--------------------|--|--|
| Twice a number is equal to 18.  |                    |  |  |
| Marcia is <i>m</i> years old. In 14 years, she will be 30.  |                    |  |  |
| 32 is equivalent to 12 more than the product of 5 and <i>c</i> .  |                    |  |  |
| A number divided by 6 is equal to 8.  |                    |  |  |
| <i>k</i> decreased by 9 is equal to 17.   |                    |  |  |
| 12 is equal to 14 less than 4 times a number.   |                    |  |  |
| A large pizza sliced into 18 pieces is<br>equally shared among <i>x</i> people, so that<br>each person gets 3 pieces.   |                    |  |  |
| Allan made a withdrawal of <i>g</i> dollars from his savings account. He had \$370 in his account and now he has \$220. |                    |  |  |

**2.** Write the inequality symbols in the table.

| Inequalities |         |  |
|--------------|---------|--|
| Symbol       | Meaning |  |
|              |         |  |
|              |         |  |
|              |         |  |
|              |         |  |
|              |         |  |

**3.** Working with your partner, write the algebraic inequality for each sentence in the table.

| Sentence   | Algebraic Inequality |  |  |
|--|----------------------|--|--|
| 11 increased by twice a number is greater than 21.   |                      |  |  |
| 6 is less than or equal to the product of <i>f</i> and 2.  |                      |  |  |
| The quotient of a number and 5 is less than 10.  |                      |  |  |
| The difference of <i>r</i> and 13 is greater than or equal to 17.  |                      |  |  |
| Mariella had \$625 in her savings account.<br>She withdrew <i>h</i> dollars from this account.<br>The bank requires customers to keep more<br>than \$250 in their savings account. |                      |  |  |

# **Trying It on Your Own**

**1.** Translate into an algebraic equation or inequality: *b* more than 3 is less than or equal to 16.

**a.**  $b + 3 \le 16$ **b.**  $b - 3 \le 16$ **c.**  $3b \le 16$ **d.**  $16 \le 3b$ 

**2.** Translate into an algebraic equation or inequality: The product of 6 and the sum of *c* and 7 is equal to 54.

**a.** 6*c* + 7 = 54 **b.** 6(7*c*) = 54 **c.** 6(*c* + 7) = 54 **d.** 6 x 7 + *c* = 54

**3.** Translate into an algebraic equation or inequality: Daria is renting a room for a meeting. She has \$400 to spend on a rental fee of \$75 plus \$5 per an unknown number of people.

a. 400 = 75 + 5m
b. 400 = 75 + 5 + m
c. 75(5m) = 400
d. (75 + 5)m = 400

**4.** Translate into an algebraic equation or inequality: 2 less than the quotient of *n* and 4 is greater than 18.

**a.** 
$$2 - \frac{n}{4} > 18$$
  
**b.**  $2 < n \div 4 > 18$   
**c.**  $\frac{n}{4} - 2 < 18$   
**d.**  $\frac{n}{4} - 2 > 18$ 

# Wrapping It Up

On your whiteboard, write a sentence(s) that might be represented by the algebraic equation 2h - 7 = 13.

# Warming Up:

Evaluate the expressions for m = -5.

**1.** *m* + 10

**2.**6*m* 

#### **3.** $-3 + m^2$

**4.**  $\frac{20}{m}$ 

**5.** 2*m* + 3*m* 

# Learning to Solve:

The formula for the area of a circle is  $A = \pi r^2$ .

**1.** Find the area of a circle with a radius of 2.4 centimeters.

 $\pi = 3.14$ 

2. The radius of a circular swimming pool is 25 feet. What is the area of the pool?

 $\pi = 3.14$ 

## **Practicing Together:**

Working with your partner, fill in the missing values in the table.

*Interest* is the amount of money you earn or owe when investing or spending money.

*Principal* is the initial amount of money invested or spent.

*Rate* is the percentage of the principal that results in the interest.

*Time* is days, weeks, months, years, etc.

To find the amount of interest on money that you have invested, you multiply the amount of money invested by the rate and by the time.

The formula for determining the simple interest on an amount of money is interest = principal  $\cdot$  rate  $\cdot$  time, which is represented by I = prt.

| Interest | Principal | Rate | Time               | Formula/Equation<br><i>I = prt</i> |
|----------|-----------|------|--------------------|------------------------------------|
|          | \$2,000   | 5%   | 5 years            |                                    |
| \$540    | \$18,000  |      | $\frac{1}{2}$ year |                                    |
| \$43.125 | \$575     | 2.5% |                    |                                    |
|          | \$135,500 | 4%   | 10 years           |                                    |

# **Trying It on Your Own**

**1.** Distance traveled is calculated by multiplying the rate of speed by the time spent traveling. Select the person who wrote the correct formula to represent this calculation.

**a.** Alex wrote the formula d = rt to represent the calculation.

**b.** Mariah wrote the formula dr = t to represent the calculation.

**c.** Madison wrote the formula  $d = \frac{r}{t}$  to represent the calculation.

**d.** Frank wrote the formula *drt* to represent the calculation.

2. Dylan drove 66 miles per hour for 3 hours. How far did he travel?

- **a.** 132 miles
- **b.** 22 miles
- **c.** 198 miles
- **d.** 68 miles
#### Name: \_

- **3.** Calculate the speed at which an airplane flies if it travels 2,100 miles in 3.5 hours.
  - **a.** 7,350 mph
  - **b.** 700 mph
  - **c.** 600 mph
  - **d.** 60 mph

**4.** Ray said that *d* = *rt* is the same as *d* = *tr*. Arthur disagrees. Who do you agree with, Ray or Arthur?

- **a.** Arthur, because you cannot switch the variables around.
- **b.** Arthur, because rate is found by multiplying the distance by the time.
- c. Ray, because distance is rate divided by time.
- **d.** Ray, because to find the distance, you multiply the rate by the time.

Name: \_\_\_\_

#### Wrapping It Up

You are given the formula:

$$\mathsf{F} = \mathsf{C}(\frac{9}{5}) + 32$$

This formula converts a Celsius temperature to a Fahrenheit temperature. Write the process you would follow to convert a temperature of 16°C to Fahrenheit.

# Notes Equations AND Expressions

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Expressions

## and quations 2

### **Extra Practice**

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5(2h+4) = 40

Simplify each expression.

**1.** 6(3 + 2*k*)

**2.** 8(2*a* – 5)

**3.** 6(5 – 4*h*)

**4.** 7(1 + (-2*y*))

Simplify each expression.

**1.** Cynthia took 2 of her friends to the movies. All 3 of them wanted a fruit snack that cost \$3.25 each and a water that cost \$1.75 each. How much did they spend altogether on their drinks and popcorn? Write the expression or equation that you could use to find the answer or solve.

**2.** Jason wanted to find the area of the rectangle below. Find 2 ways that he could use. Find the area.



**3.** Josh simplified a problem.

| 40(15 + 7)     |
|----------------|
| 15(40) + 7(40) |
| 600 + 280      |

880

Do you agree with Josh's work? Why or why not?

**4.** Simplify: (15 + 8)20

Evaluate each expression for the given value of the variable.

|                                    | x = 4 | <i>x</i> = 0 | x = -3 | x = -1 |
|------------------------------------|-------|--------------|--------|--------|
| 4(x+3) - 2x                        |       |              |        |        |
| $\frac{-6(3-x)}{2} + x$            |       |              |        |        |
| 7x - 2(x - 5)                      |       |              |        |        |
| $\frac{4x}{2} + \frac{2(3x-1)}{2}$ |       |              |        |        |
| $12 - 3x + \frac{6x}{3}$           |       |              |        |        |

**1.** Graph the solution to the inequality on the number line: n + 2 < 8



**2.** Graph the solution to the inequality on the number line:  $18 + 7x \ge 32$ 





Solve each equation.

**1.** 6*y* + 14 = 11

**2.** 
$$16 = \frac{1}{2}(h+24)$$

**3.** 4 = 4(k + 5)

**4.** 3(4 – *x*) = 36

The formula for the volume of a rectangular prism is V = lwh, where l = length, w = width, h = height. Use the formula to solve problems 1 and 2.

**1.** A rectangular prism has a volume of 360 cubic inches. The length is 2 inches and the height is 15 inches. What is the measure of the width?

**2.** A rectangular prism has a volume of 800 cubic feet. The width is 8 feet and the height is 10 feet. What is the measure of the length?

The formula for the area of a trapezoid is  $A = \frac{1}{2}(b_1 + b_2)h$  where  $b_1$  and  $b_2$  = the two bases and h = height. Use the formula to solve problems 3 and 4.

**3.** A trapezoid has  $b_1 = 3$  inches and  $b_2 = 5$  inches. The area is 24 square inches. What is the measure of the height?

**4.** The area of a trapezoid is 50 square centimeters. The height is 5 centimeters and b1 is 8 centimeters. What is the measure of the other base  $(b_2)$ ?

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|      |              |                 |                                    |                       |            |                                      |   |        |   |   |   |

| Name:              | Number Correct:  |                    |                 |
|--------------------|------------------|--------------------|-----------------|
| 1 8                | <b>2</b> 1 × 7   | <b>3</b> 5         | <b>4</b> 6      |
| × 2                |                  | × 8                | × 3             |
| <b>5</b> 7         | 6 6              | <b>7</b> 2         | <b>8</b> 4 × 5  |
| × 4                | × 6              | × 12               |                 |
| 9 7                | <b>10</b> 3 × 9  | <b>11</b> 11       | <b>12</b> 3     |
| × 6                |                  | × 5                | × 3             |
| <b>13</b> 8        | <b>14</b> 2      | <b>15</b> 6        | <b>16</b> 4     |
| × 9                | × 4              | × 9                | × 12            |
| <b>17</b> 9<br>× 6 | <b>18</b> 10 × 8 | <b>19</b> 2<br>× 9 | <b>20</b> 8 × 3 |

| Name:          |                     |              |                 |
|----------------|---------------------|--------------|-----------------|
| Multiplication | n Timed Practice Sl | heet 2       | Number Correct: |
| 1 7            | <b>2</b> 5          | <b>3</b> 9   | <b>4</b> 7      |
| × 2            | × 5                 | × 1          | × 11            |
| 5 5            | 6 10                | <b>7</b> 7   | <b>8</b> 3      |
| × 6            | × 3                 | × 5          | × 4             |
| <b>9</b> 4 × 9 | <b>10</b> 4         | <b>11</b> 12 | <b>12</b> 7     |
|                | × 7                 | × 6          | × 8             |
| <b>13</b> 7    | <b>14</b> 8         | <b>15</b> 6  | <b>16</b> 5     |
| × 10           | × 6                 | <u>× 7</u>   | × 3             |
| <b>17</b> 9    | <b>18</b> 6         | <b>19</b> 9  | <b>20</b> 8 × 4 |
| × 8            | × 4                 | × 4          |                 |

| Name:       |                |                   |                 |  |
|-------------|----------------|-------------------|-----------------|--|
| <b>1</b> 1  | <b>2</b> 4 × 3 | <b>3</b> 5        | <b>4</b> 10     |  |
| <u>× 12</u> |                | × 2               | <u>× 7</u>      |  |
| 5 10<br>× 2 | <b>6</b> 4 × 8 | <b>7</b> 3<br>× 7 | <b>8</b> 12 × 7 |  |
| <b>9</b> 11 | <b>10</b> 3    | <b>11</b> 4       | <b>12</b> 5     |  |
| × 6         | × 12           | <u>× 6</u>        | × 9             |  |
| <b>13</b> 8 | <b>14</b> 7    | <b>15</b> 8       | <b>16</b> 5     |  |
| × 7         | × 3            | × 8               | × 10            |  |
| <b>17</b> 5 | <b>18</b> 9    | <b>19</b> 3       | <b>20</b> 9 × 7 |  |
| × 4         | × 2            | × 11              |                 |  |

| Name:  | lame:              |                    |                   |  |  |
|--|--------------------|--------------------|-------------------|--|--|
| Multiplication Timed Practice Sheet 4         Number Correct |                    |                    |                   |  |  |
| 1 2  | <b>2</b> 3         | <b>3</b> 8         | 4 2               |  |  |
| × 8  | × 6                | × 5                | × 7               |  |  |
| <b>5</b> 11 × 9  | 6 4                | 7 9                | <b>8</b> 3        |  |  |
|  | × 4                | × 4                | × 10              |  |  |
| <b>9</b> 5   | <b>10</b> 5        | 11 7               | <b>12</b> 1 × 5   |  |  |
| × 9  | × 12               | × 3                |                   |  |  |
| <b>13</b> 3  | <b>14</b> 6        | <b>15</b> 9        | <b>16</b> 4 × 5   |  |  |
| × 2  | × 8                | × 11               |                   |  |  |
| <b>17</b> 12 × 5   | <b>18</b> 4<br>× 2 | <b>19</b> 7<br>× 7 | <b>20</b> 10 × 10 |  |  |

| Name:         Multiplication Timed Practice Sheet 5         Number Correct: |                  |                    |                  |
|---|------------------|--------------------|------------------|
| 1 4   | <b>2</b> 9       | <b>3</b> 5         | <b>4</b> 10      |
| × 6   | × 3              | × 11               | × 5              |
| 5 5   | 6 2              | 7 3                | <b>8</b> 12      |
| × 7   | × 10             | × 1                | × 5              |
| 9 8   | <b>10</b> 6      | 11 6               | <b>12</b> 7      |
| × 6   | × 12             | × 2                | × 7              |
| <b>13</b> 4   | <b>14</b> 5      | <b>15</b> 3        | <b>16</b> 12 × 2 |
| × 7   | × 3              | × 8                |                  |
| <b>17</b> 9<br>× 3  | <b>18</b> 11 × 4 | <b>19</b> 7<br>× 4 | <b>20</b> 9 × 10 |

| Name:<br>Multiplication | Number Correct:     |                     |                   |
|-------------------------|---------------------|---------------------|-------------------|
| 1 4                     | <b>2</b> 3          | <b>3</b> 7          | <b>4</b> 6        |
| × 3                     | × 6                 | × 5                 | × 4               |
| 5 8                     | 6 2                 | 7 11                | <b>8</b> 5        |
| × 10                    | × 2                 | × 2                 | × 5               |
| <b>9</b> 3              | <b>10</b> 4 × 8     | <b>11</b> 7         | <b>12</b> 8       |
| × 5                     |                     | × 9                 | × 12              |
| <b>13</b> 2<br>× 10     | <b>14</b> 1 × 8     | <b>15</b> 6<br>× 11 | <b>16</b> 11 × 12 |
| <b>17</b> 12 × 8        | <b>18</b> 10<br>× 6 | <b>19</b> 2<br>× 5  | <b>20</b> 9 × 7   |

| Name:              | lame:              |                  |                 |  |
|--------------------|--------------------|------------------|-----------------|--|
| Multiplication     | Timed Practice Sh  | Number Correct:  |                 |  |
| 1 5                | <b>2</b> 4 × 4     | <b>3</b> 5       | 4 9             |  |
| × 8                |                    | × 7              | × 2             |  |
| <b>5</b> 8         | 6 3                | 7 2              | <b>8</b> 3      |  |
| <u>× 11</u>        | × 7                | × 6              | <u>× 5</u>      |  |
| <b>9</b> 3         | <b>10</b> 9 × 12   | <b>11</b> 6      | <b>12</b> 8     |  |
| × 4                |                    | × 10             | × 3             |  |
| <b>13</b> 12       | <b>14</b> 8        | <b>15</b> 5      | <b>16</b> 1     |  |
| × 11               | × 8                | × 4              | <u>× 11</u>     |  |
| <b>17</b> 6<br>× 7 | <b>18</b> 7<br>× 6 | <b>19</b> 10 × 9 | <b>20</b> 6 × 5 |  |

| Iame:         Multiplication Timed Practice Sheet 8         Number Correct: |              |             |                 |  |
|---|--------------|-------------|-----------------|--|
| 1 3   | <b>2</b> 9   | <b>3</b> 11 | <b>4</b> 6      |  |
| × 10  | × 6          | × 2         | × 10            |  |
| 5 7   | 6 8          | 7 5         | <b>8</b> 4      |  |
| × 9   | × 7          | × 2         | <u>× 11</u>     |  |
| <b>9</b> 4  | <b>10</b> 6  | <b>11</b> 6 | <b>12</b> 8     |  |
| × 1   | × 9          | × 5         | × 5             |  |
| <b>13</b> 10  | <b>14</b> 11 | <b>15</b> 2 | <b>16</b> 9     |  |
| × 3   | <u>× 7</u>   | × 12        | × 9             |  |
| <b>17</b> 6   | <b>18</b> 2  | <b>19</b> 7 | <b>20</b> 4 × 2 |  |
| × 8   | × 3          | × 12        |                 |  |
| Name:<br>Multiplication | Timed Practice Sh | neet 9              | Number Correct:    |
|-------------------------|-------------------|---------------------|--------------------|
| 1 6                     | <b>2</b> 9        | <b>3</b> 11         | 4 2                |
| × 2                     | × 5               | × 8                 | × 6                |
| <b>5</b> 5              | <b>6</b> 8        | 7 9                 | <b>8</b> 10 × 4    |
| <u>× 6</u>              | × 9               | × 8                 |                    |
| <b>9</b> 12 × 3         | <b>10</b> 11 × 11 | <b>11</b> 4<br>× 10 | <b>12</b> 7<br>× 8 |
| <b>13</b> 3             | <b>14</b> 4       | <b>15</b> 8         | <b>16</b> 12 × 9   |
| × 9                     | × 9               | × 2                 |                    |
| <b>17</b> 11 × 3        | <b>18</b> 10 × 7  | <b>19</b> 1 × 6     | <b>20</b> 2 × 8    |

| Name:            |                    |                   |                  |
|------------------|--------------------|-------------------|------------------|
| Multiplication   | Timed Practice Sh  | neet 10           | Number Correct:  |
| 1 3              | <b>2</b> 6         | <b>3</b> 3        | <b>4</b> 10      |
| × 8              | × 3                | × 3               | × 1              |
| 5 2              | <b>6</b> 2         | <b>7</b> 9        | <b>8</b> 9       |
| × 5              | <u>× 11</u>        | × 9               | × 5              |
| <b>9</b> 2       | <b>10</b> 6        | 11 2              | <b>12</b> 12 × 3 |
| × 9              | × 6                | × 3               |                  |
| <b>13</b> 2      | <b>14</b> 12       | <b>15</b> 8       | <b>16</b> 11 × 8 |
| × 7              | × 10               | × 4               |                  |
| <b>17</b> 11 × 4 | <b>18</b> 5<br>× 5 | <b>19</b> 10 × 11 | <b>20</b> 7 × 2  |

| Name:<br>Division Timed | Practice Sheet 1 |                | Number Correct: |
|-------------------------|------------------|----------------|-----------------|
| <b>1</b> 7)21           | <b>2</b> 5)10    | <b>3</b> 2)14  | <b>4</b> 9)27   |
| <b>5</b> 6) 24          | <b>6</b> 10)70   | <b>7</b> 8)32  | <b>8</b> 6) 36  |
| <b>9</b> 3)9            | <b>10</b> 5) 35  | <b>11</b> 1) 8 | <b>12</b> 12)24 |
| <b>13</b> 2)20          | <b>14</b> 8)40   | <b>15</b> 3)15 | <b>16</b> 4)32  |
| <b>17</b> 4)28          | <b>18</b> 7)42   | <b>19</b> 9)63 | <b>20</b> 6)66  |
|                         |                  |                |                 |

| Name:<br>Divis | sion Timed P | Practice Sheet 2 |                 | Number Correct: |
|----------------|--------------|------------------|-----------------|-----------------|
| 1              | 2)10         | <b>2</b> 3)27    | <b>3</b> 3)21   | <b>4</b> 7)14   |
| 5              | 6)30         | <b>6</b> 1) 6    | <b>7</b> 6) 54  | <b>8</b> 12)60  |
| 9              | 3 36         | <b>10</b> 4)24   | <b>11</b> 5)25  | <b>12</b> 10)80 |
| 13             | 8)16         | <b>14</b> 11)44  | <b>15</b> 8) 24 | <b>16</b> 5)30  |
| 17             | 9) 54        | <b>18</b> 6)60   | <b>19</b> 8)72  | <b>20</b> 7)56  |
|                |              |                  |                 |                 |

| Name:<br>Division Timed | d Practice Sheet 3 |                | Number Correct:  |
|-------------------------|--------------------|----------------|------------------|
| <b>1</b> 11)66          | <b>2</b> 2)18      | <b>3</b> 6)42  | <b>4</b> 7)63    |
| <b>5</b> 5)45           | <b>6</b> 3)24      | <b>7</b> 9)36  | <b>8</b> 1)12    |
| <b>9</b> 4)20           | <b>10</b> 10)30    | <b>11</b> 9)36 | <b>12</b> 9)90   |
| <b>13</b> 8) 80         | <b>14</b> 3)18     | <b>15</b> 8)24 | <b>16</b> 4)16   |
| <b>17</b> 7)35          | <b>18</b> 6) 18    | <b>19</b> 9)99 | <b>20</b> 12)120 |
|                         |                    |                |                  |

| Divis | ion Timed Pr | Number Correct: |       |                 |                 |
|-------|--------------|-----------------|-------|-----------------|-----------------|
| 1     | 5)15         | 2               | 11)55 | <b>3</b> 4)12   | <b>4</b> 9)45   |
| 5     | 7)28         | 6               | 4)36  | <b>7</b> 1)7    | <b>8</b> 10)60  |
| 9     | 2)16         | 10              | 5)40  | <b>11</b> 8) 56 | <b>12</b> 2)24  |
| 13    | 9)18         | 14              | 11)88 | <b>15</b> 12)48 | <b>16</b> 7)49  |
| 17    | 7)56         | 18              | 3 6   | <b>19</b> 4)40  | <b>20</b> 6) 30 |
|       |              |                 |       |                 |                 |

| Division Time   | ed Practice Sheet 5 |                 | Number Correct: |
|-----------------|---------------------|-----------------|-----------------|
| <b>1</b> 3)21   | <b>2</b> 6)12       | <b>3</b> 3)36   | <b>4</b> 3)15   |
| <b>5</b> 9)36   | <b>6</b> 8)48       | <b>7</b> 3)12   | <b>8</b> 10)90  |
| <b>9</b> 4)24   | <b>10</b> 5)60      | <b>11</b> 11)33 | <b>12</b> 8)64  |
| <b>13</b> 1)4   | <b>14</b> 4)28      | <b>15</b> 6) 48 | <b>16</b> 5) 55 |
| <b>17</b> 12)24 | <b>18</b> 7)70      | <b>19</b> 9)27  | <b>20</b> 12)96 |
|                 |                     |                 |                 |

| Name:       | Name:       |              |         |    |       |            |             |
|-------------|-------------|--------------|---------|----|-------|------------|-------------|
| Divisior    | n Timed Pra | ctice        | Sheet 6 |    |       | Numbe      | er Correct: |
| 1 2         | 20          | 2            | 8)16    | 3  | 5)20  | 4          | 1)3         |
| <b>5</b> 5  | 35          | 6            | 4)44    | 7  | 6)48  | <b>8</b> 1 | 1)110       |
| <b>9</b> 3  | ) 18        | 10           | 2 4     | 11 | 3)27  | 12         | 6)72        |
| <b>13</b> 9 | 81          | 14           | 3)24    | 15 | 10)20 | 16         | 4)48        |
| <b>17</b> 6 | 30          | <b>18</b> 10 | 0)110   | 19 | 9)54  | 20         | 7)28        |
|             |             |              |         |    |       |            |             |

| Name: |              |         |           |    |       |                 |
|-------|--------------|---------|-----------|----|-------|-----------------|
| Divis | sion Timed P | ractice | e Sheet 7 |    |       | Number Correct: |
| 1     | 2)10         | 2       | 8)40      | 3  | 3 9   | <b>4</b> 11)55  |
| 5     | 8)56         | 6       | 8)32      | 7  | 7)63  | 8 2)22          |
| 9     | 4)36         | 10      | 10)80     | 11 | 8)64  | <b>12</b> 12)72 |
| 13    | 5)15         | 14      | 9)63      | 15 | 7)77  | <b>16</b> 6)18  |
| 17    | 5)50         | 18      | 6) 36     | 19 | 6) 24 | <b>20</b> 1)9   |
|       |              |         |           |    |       |                 |

| Name:                 |                  |                  |                 |
|-----------------------|------------------|------------------|-----------------|
| <b>Division Timed</b> | Practice Sheet 8 |                  | Number Correct: |
| <b>1</b> 9)45         | <b>2</b> 11)66   | <b>3</b> 2) 4    | <b>4</b> 2)12   |
| <b>5</b> 1) 5         | <b>6</b> 12)108  | <b>7</b> 5) 55   | 8 7)49          |
| <b>9</b> 5)60         | <b>10</b> 4) 8   | <b>11</b> 4)32   | <b>12</b> 10)40 |
| <b>13</b> 7)84        | <b>14</b> 7)21   | <b>15</b> 12)144 | <b>16</b> 6) 54 |
| <b>17</b> 9)81        | <b>18</b> 11)99  | <b>19</b> 4)40   | <b>20</b> 5)50  |
|                       |                  |                  |                 |

Number Correct:

| 1  | 11)22 | <b>2</b> 4)12  | <b>3</b> 6) 66  | <b>4</b> 5)30   |    |
|----|-------|--|---|-----------------|----|
| 5  | 4)16  | <b>6</b> 2) 6  | <b>7</b> 5)45   | <b>8</b> 10)120 |    |
| 9  | 10)40 | <b>10</b> 8) 88  | <b>11</b> 8)72  | <b>12</b> 12)36 |    |
| 13 | 2)14  | <b>14</b> 11)121   | <b>15</b> 7)35  | <b>16</b> 1)10  |    |
| 17 | 4)48  | <b>18</b> 9)72   | <b>19</b> 12)84   | <b>20</b> 3)33  |    |
|    |       |  |   |                 |    |
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Name: \_\_\_\_\_

**Division Timed Practice Sheet 9** 

| Name:<br>Division Time | d Practice Sheet 10 |    |       | Number Correct: |
|------------------------|---------------------|----|-------|-----------------|
| <b>1</b> 10)70         | <b>2</b> 6)12       | 3  | 2)8   | <b>4</b> 3)12   |
| <b>5</b> 5)25          | <b>6</b> 6) 42      | 7  | 5)20  | 8 3)30          |
| <b>9</b> 2)18          | <b>10</b> 10)100    | 11 | 4) 12 | <b>12</b> 8)48  |
| <b>13</b> 7)42         | <b>14</b> 12)36     | 15 | 4)48  | <b>16</b> 11)77 |
| <b>17</b> 9)72         | <b>18</b> 1)11      | 19 | 3)33  | <b>20</b> 5)10  |
|                        |                     |    |       |                 |

| Jame:              |                    |                    | Number Correct      |
|--------------------|--------------------|--------------------|---------------------|
| 1 4<br><u>× 7</u>  | <b>2</b> 2)16      | <b>3</b> 4 × 5     | <b>4</b> 7)21       |
| 5 11<br><u>× 1</u> | <b>6</b> 7)56      | 7 8<br>× 8         | <b>8</b> 3<br>× 4   |
| <b>9</b> 4)36      | <b>10</b> 3)18     | <b>11</b> 8)64     | <b>12</b> 3<br>× 12 |
| <b>13</b> 9)45     | <b>14</b> 7)70     | <b>15</b> 7<br>× 6 | <b>16</b> 10 × 6    |
| <b>17</b> 8<br>× 2 | <b>18</b> 9<br>× 6 | <b>19</b> 5)20     | <b>20</b> 5) 55     |

| Name:                              |   |  |  |
|------------------------------------|---|--|--|
| Mixed Facts Timed Practice Sheet 2 |   |  |  |
| <b>2</b> 5<br>× 10                 | <b>3</b> 2)12   | <b>4</b> 5<br>× 7  |  |
| <b>6</b> 11 × 4                    | 7 7<br>× 8  | <b>8</b> 8) 32   |  |
| <b>10</b> 3)33                     | <b>11</b> 5<br>× 12   | <b>12</b> 1)12   |  |
| <b>14</b> 4)16                     | <b>15</b> 6<br>× 9  | <b>16</b> 3<br>× 6   |  |
| <b>18</b> 3<br>× 8                 | <b>19</b> 10)20   | <b>20</b> 4 8  |  |
|                                    | ed Practice Sheet 2<br>2 $5$<br>$\times 10$<br>6 $11$<br>$\times 4$<br>10 $3\overline{)33}$<br>14 $4\overline{)16}$<br>18 $3$<br>$\times 8$ | a $2$ $5$ $3$ $2\sqrt{12}$ 6       11       7       7 $4$ 7 $7$ $\times 8$ 10 $3\sqrt{33}$ 11 $5$ 14 $4\sqrt{16}$ 15 $6$ $\times 8$ 19 $10\sqrt{20}$ |  |

| Name:                  |                     |                   |                   |
|------------------------|---------------------|-------------------|-------------------|
| <b>Mixed Facts Tim</b> | ed Practice Sheet 3 | 3                 | Number Correct:   |
| 1 8<br>× 5             | <b>2</b> 3)12       | <b>3</b> 4<br>× 8 | <b>4</b> 8)56     |
| 5 7<br>× 7             | <b>6</b> 10)60      | <b>7</b> 4) 8     | <b>8</b> 6<br>× 1 |
| <b>9</b> 10)100        | <b>10</b> 9 × 2     | <b>11</b> 9)99    | <b>12</b> 3 × 5   |
| <b>13</b> 10 × 11      | <b>14</b> 5<br>× 2  | <b>15</b> 3)27    | <b>16</b> 12 × 4  |
| <b>17</b> 8)40         | <b>18</b> 7<br>× 9  | <b>19</b> 5)35    | <b>20</b> 12)36   |
|                        |                     |                   |                   |

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| Name:                              |                    |                    |                    |
|------------------------------------|--------------------|--------------------|--------------------|
| Mixed Facts Timed Practice Sheet 4 |                    |                    | Number Correct:    |
| 1 4<br>× 6                         | <b>2</b> 5)40      | <b>3</b> 2<br>× 11 | <b>4</b> 3)21      |
| <b>5</b> 1) 7                      | 6 12<br>× 6        | <b>7</b> 4)12      | 8 2<br>× 10        |
| 9 6<br>× 8                         | <b>10</b> 5)50     | 11 3<br>× 3        | <b>12</b> 9)72     |
| <b>13</b> 8<br>× 10                | <b>14</b> 7<br>× 4 | <b>15</b> 11)99    | <b>16</b> 5<br>× 9 |
| <b>17</b> 12)60                    | <b>18</b> 6) 36    | <b>19</b> 3<br>× 5 | <b>20</b> 7)28     |
|                                    |                    |                    |                    |

| Name:              | Name:               |                   |                    |  |
|--------------------|---------------------|-------------------|--------------------|--|
| Mixed Facts Time   | ed Practice Sheet 5 | •                 | Number Correct:    |  |
| 1 10<br>× 2        | <b>2</b> 3<br>× 11  | <b>3</b> 3)15     | <b>4</b> 11)55     |  |
| <b>5</b> 12)24     | 6 7<br>× 5          | 7 9<br>× 1        | <b>8</b> 9<br>× 7  |  |
| 9 8<br>× 4         | <b>10</b> 11 × 7    | <b>11</b> 3)12    | <b>12</b> 4)20     |  |
| <b>13</b> 7)35     | <b>14</b> 9)36      | <b>15</b> 12 × 10 | <b>16</b> 8<br>× 9 |  |
| <b>17</b> 9<br>× 9 | <b>18</b> 8)48      | <b>19</b> 6)60    | <b>20</b> 4)24     |  |
|                    |                     |                   |                    |  |

| Name:                              |                    |                    |                     |
|------------------------------------|--------------------|--------------------|---------------------|
| Mixed Facts Timed Practice Sheet 6 |                    |                    | Number Correct:     |
| 1 3<br>× 9                         | <b>2</b> 5)30      | <b>3</b> 4)28      | <b>4</b> 10 × 8     |
| 5 8<br>× 7                         | 6 7<br>× 3         | <b>7</b> 2)20      | <b>8</b> 5) 25      |
| <b>9</b> 6)24                      | <b>10</b> 2 × 12   | <b>11</b> 11 × 2   | <b>12</b> 12)48     |
| <b>13</b> 1)11                     | <b>14</b> 11)44    | <b>15</b> 9<br>× 9 | <b>16</b> 5<br>× 3  |
| <b>17</b> 5)15                     | <b>18</b> 9<br>× 4 | <b>19</b> 6) 48    | <b>20</b> 3<br>× 10 |
|                                    |                    |                    |                     |

| Name:                     |                   |                    |                    |
|---------------------------|-------------------|--------------------|--------------------|
| <b>Mixed Facts Time</b>   |                   | Number Correct:    |                    |
| 1 5<br>× 4                | <b>2</b> 4)32     | <b>3</b> 8<br>× 3  | <b>4</b> 7)14      |
| <b>5</b> 3)30             | <b>6</b> 7)42     | <b>7</b> 6) 30     | 8 6<br>× 7         |
| 9 6<br>× 4                | <b>10</b> 4)40    | <b>11</b> 7<br>× 1 | <b>12</b> 5<br>× 8 |
| <b>13</b> 9)81            | <b>14</b> 10 × 12 | <b>15</b> 9)63     | <b>16</b> 4<br>× 9 |
| <b>17</b> 6<br><u>× 2</u> | <b>18</b> 11 × 3  | <b>19</b> 11)22    | <b>20</b> 10)70    |

| Name:                              |                    |                     |                    |
|------------------------------------|--------------------|---------------------|--------------------|
| Mixed Facts Timed Practice Sheet 8 |                    |                     | Number Correct:    |
| <b>1</b> 10 × 4                    | <b>2</b> 3)24      | <b>3</b> 5)45       | <b>4</b> 9<br>× 3  |
| 5 6<br><u>× 11</u>                 | 6 6<br>× 5         | <b>7</b> 10)40      | <b>8</b> 1) 5      |
| <b>9</b> 8)24                      | <b>10</b> 3)36     | <b>11</b> 11 × 9    | <b>12</b> 6)18     |
| <b>13</b> 12)72                    | <b>14</b> 9<br>× 8 | <b>15</b> 9) 54     | <b>16</b> 8<br>× 6 |
| <b>17</b> 7)14                     | <b>18</b> 6<br>× 7 | <b>19</b> 7<br>× 12 | <b>20</b> 5<br>× 5 |
|                                    |                    |                     |                    |

| Name:                  |                                    |                     |                    |
|------------------------|------------------------------------|---------------------|--------------------|
| <b>Mixed Facts Tin</b> | Mixed Facts Timed Practice Sheet 9 |                     |                    |
| 1 4<br>× 4             | <b>2</b> 9)18                      | <b>3</b> 9<br>× 5   | <b>4</b> 3)12      |
| <b>5</b> 9)27          | 6 11<br>× 11                       | <b>7</b> 5)60       | <b>8</b> 6)12      |
| <b>9</b> 6)60          | <b>10</b> 5<br>× 6                 | <b>11</b> 12<br>× 8 | <b>12</b> 8<br>× 1 |
| <b>13</b> 7)49         | <b>14</b> 6<br>× 2                 | <b>15</b> 11 × 10   | <b>16</b> 7)77     |
| <b>17</b> 7<br>× 10    | <b>18</b> 11)121                   | <b>19</b> 8)16      | <b>20</b> 4 × 12   |

| Name:                  |                           |                    |                   |
|------------------------|---------------------------|--------------------|-------------------|
| <b>Mixed Facts Tin</b> | Number Correct:           |                    |                   |
| 1 3<br>× 6             | <b>2</b> 10<br><u>× 7</u> | <b>3</b> 2)18      | <b>4</b> 11)88    |
| 5 7<br>× 2             | <b>6</b> 4) 48            | 7 9<br>× 10        | <b>8</b> 8)72     |
| <b>9</b> 4 × 3         | <b>10</b> 7)63            | <b>11</b> 3<br>× 7 | <b>12</b> 11 × 6  |
| <b>13</b> 3 9          | <b>14</b> 12)96           | <b>15</b> 1)10     | <b>16</b> 5)15    |
| <b>17</b> 10)90        | <b>18</b> 9<br>× 12       | <b>19</b> 2<br>× 5 | <b>20</b> 11 × 12 |
|                        |                           |                    |                   |



**Fact Practice Graph** 

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